

GEOMETRY & PHYSICS SEMINAR

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The conformal limit and projective structures

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Abstract:

In this talk we will study a gauge-theoretic construction of (branched) complex projective structures on a closed Riemann surface X of genus $g \geq 2$. This construction underlies the celebrated conformal limit of Gaiotto and provides a preliminary understanding of its geometry.

More concretely, the non-abelian Hodge correspondence maps a polystable $SL(2, \mathbb{R})$ -Higgs bundle on X to a connection which, in some cases, is the holonomy of a branched hyperbolic structure. (This happens for example in the Hitchin component.) On the other hand, Gaiotto's conformal limit then maps the same bundle to a partial oper, i.e., to a connection whose holonomy is that of a branched complex projective structure compatible with X . We will see how these are both instances of the same phenomenon, i.e. that the family of connections appearing in the conformal limit can be understood as a family of complex projective structures, deforming the hyperbolic ones into the ones compatible with X . For zero Toledo invariant, this deformation turns out to be optimal, inducing a geodesic on Teichmüller's space. This is joint work with Peter B. Gothen.