

Faculdade de Ciências da Universidade de Lisboa  
cmafcio@fc.ul.pt Tel. (+351) 21 750 00 27

## SEMINÁRIO DE ANÁLISE E EQUAÇÕES DIFERENCIAIS

**Dia 14 de Julho (quinta-feira), às 13H30, na sala 6.2.33**

### Remarks on the Ambrosetti-Prodi periodic problem

**Elisa Sovrano**

**(University of Udine)**

**Abstract:**

In 2011 a very interesting note of Antonio Ambrosetti in honor of Giovanni Prodi appeared along with a list of open questions about global inversion theorems and their applications. One of these questions regards the study of the periodic Ambrosetti-Prodi problem for an ordinary differential second order equation. Our contribution to this problem concerns the study of the equation:  $u'' + f(u) = p(t)$  where  $p(t)$  is a  $T$ -periodic stepwise forcing term and the nonlinearity  $f$  is a locally Lipschitz continuous function such that  $f(0) = 0$ ,  $f(s) > 0$  for all  $s \neq 0$ ,  $\lim_{s \rightarrow \pm\infty} f(s) = +\infty$  and it is strictly decreasing for  $s \leq 0$  and strictly increasing for  $s \geq 0$ . Assuming that the nonlinear term is a positive function with global minimum at zero which satisfies the previous growth conditions, we prove under suitable conditions on  $p(t)$  the existence of infinitely many periodic solution. Moreover, we show the presence of chaotic-like dynamics via topological methods. Joint work with Fabio Zanolin (Univ. Udine).

*Seminário financiado por Fundos Nacionais através da FCT – Fundação para a Ciência e a Tecnologia no âmbito do projeto UID/MAT/04561/2013*